

Properties of QGP: A lattice perspective

- Introduction:
 T, gT, g^2T, \dots
- Bulk thermodynamics
the equation of state: QCD and SU(3)
- Heavy quark free energies
running coupling and heavy-light bound states
- Hadronic fluctuations
quark number and charge fluctuations
- Conclusions

Thermal scales in QCD

- the hard scale: $\textcolor{blue}{p} \sim \textcolor{blue}{T}$
thermal modes, bulk thermodynamics, eg. pressure

$$\frac{p}{T^4} = a_{SB} f_p(g(T))$$

- the soft scale: $\textcolor{blue}{p} \sim g\textcolor{blue}{T}$
static color-electric modes, eg. Debye screening

$$\frac{m_D(T)}{g(T)T} = \sqrt{\frac{N_c}{3} + \frac{n_f}{6} + \frac{n_f}{2\pi^2} \left(\frac{\mu_q}{T}\right)^2} \cdot f_E(g(T))$$

- the ultra-soft scale: $\textcolor{blue}{p} \sim g^2 T$
static color-magnetic modes, eg. spatial string tension

$$\frac{\sqrt{\sigma_s}}{g^2(T)T} = c_M f_M(g(T))$$

Non-thermal scales in thermal QCD

- even harder scales: $p \gg T, r^{-1} \gg T, M \gg T$
short distance physics, eg. quarkonium
$$g^2(r, T)$$
- quantitative questions, eg.
When does T become the dominant scale?

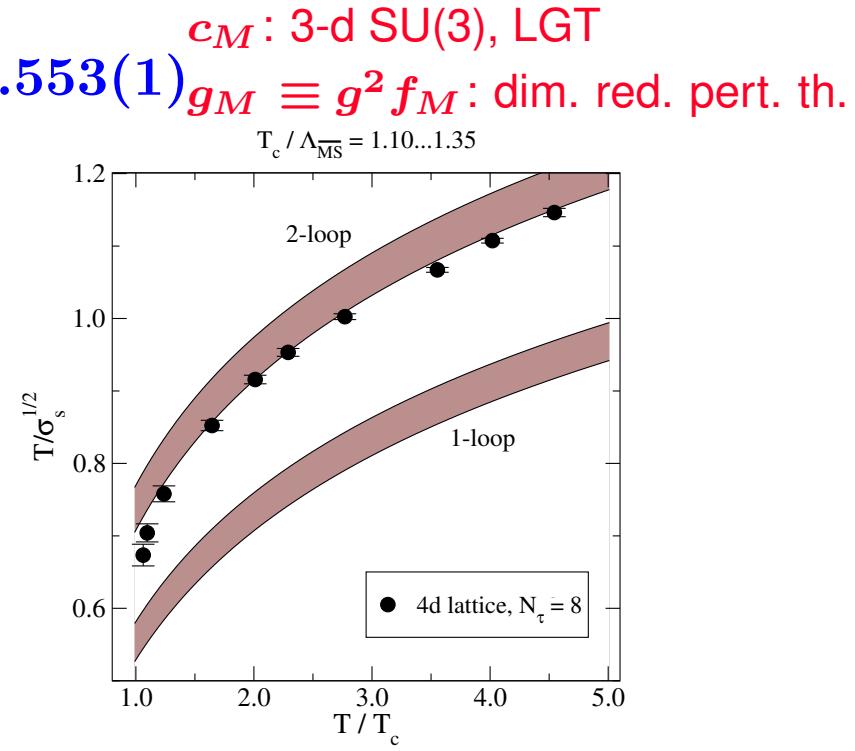
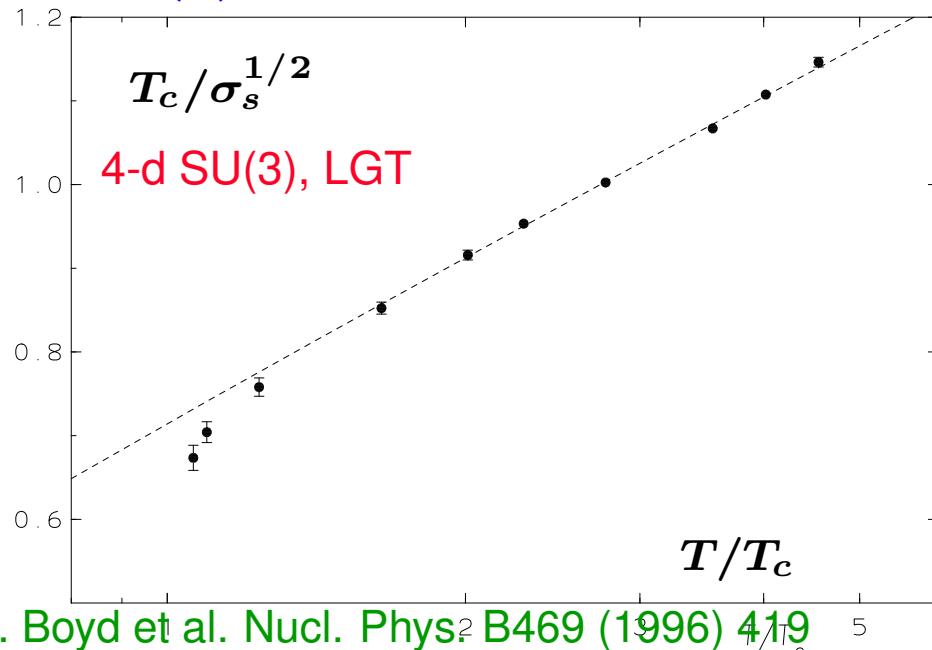
-
- Perturbation theory provides a hierarchy of length scales
 $T \gg gT \gg g^2 T \dots \Rightarrow$ guiding principle for effective theories,
resummation, dimensional reduction...
 - Early lattice results show that $g^2(T) > 1$ even at $T \sim 5T_c$
G. Boyd et al, NP B469 (1996) 419: SU(3) thermodynamics..
...one has to conclude that the temperature dependent running coupling has to be large, $g^2(T) \simeq 2$ even at $T \simeq 5T_c$
 - the Debye screening mass is large close to T_c
 - the spatial string tension does not vanish above T_c
 $\sqrt{\sigma_s} \neq 0 \Rightarrow$ the QGP is "non-perturbative" up to very high T

The spatial string tension

- Non-perturbative, vanishes in high-T perturbation theory:

$$\sqrt{\sigma_s} = - \lim_{R_x, R_y \rightarrow \infty} \ln \frac{W(R_x, R_y)}{R_x R_y}$$

- $\frac{\sqrt{\sigma_s}}{g^2(2)T} = c_M f_M(g(T))$, $c_M = 0.553(1)$
- c_M : 3-d SU(3), LGT
 $g_M \equiv g^2 f_M$: dim. red. pert. th.

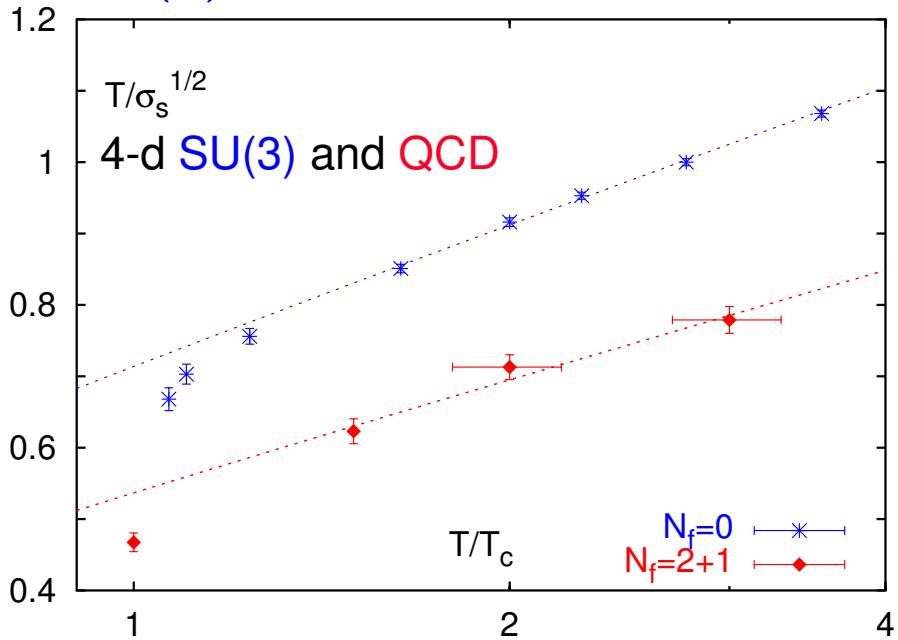


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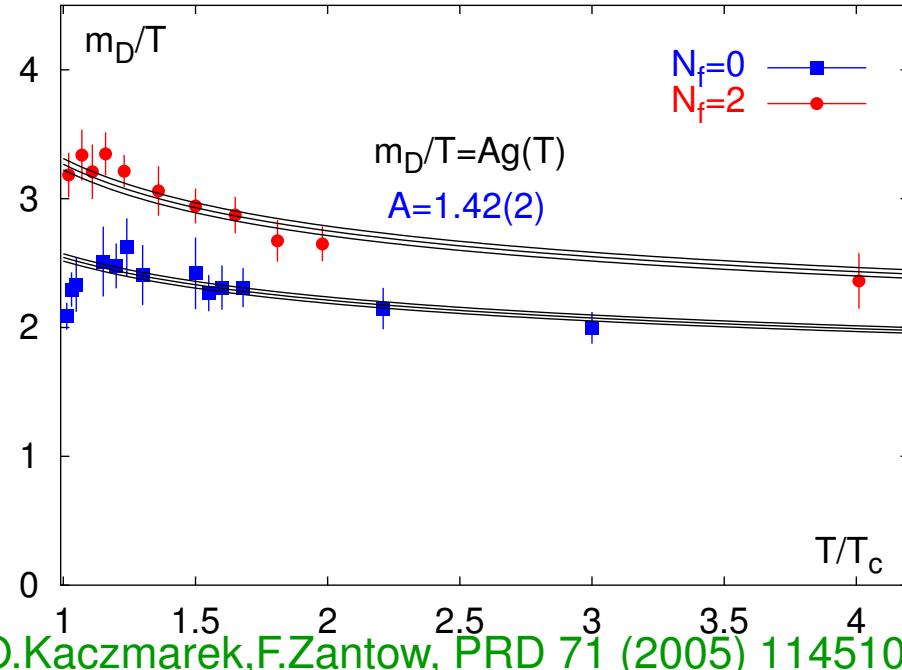


dimensional reduction works for $T \gtrsim 2T_c$
- c_M (almost) flavor independent
- $g^2(T)$ shows 2-loop running

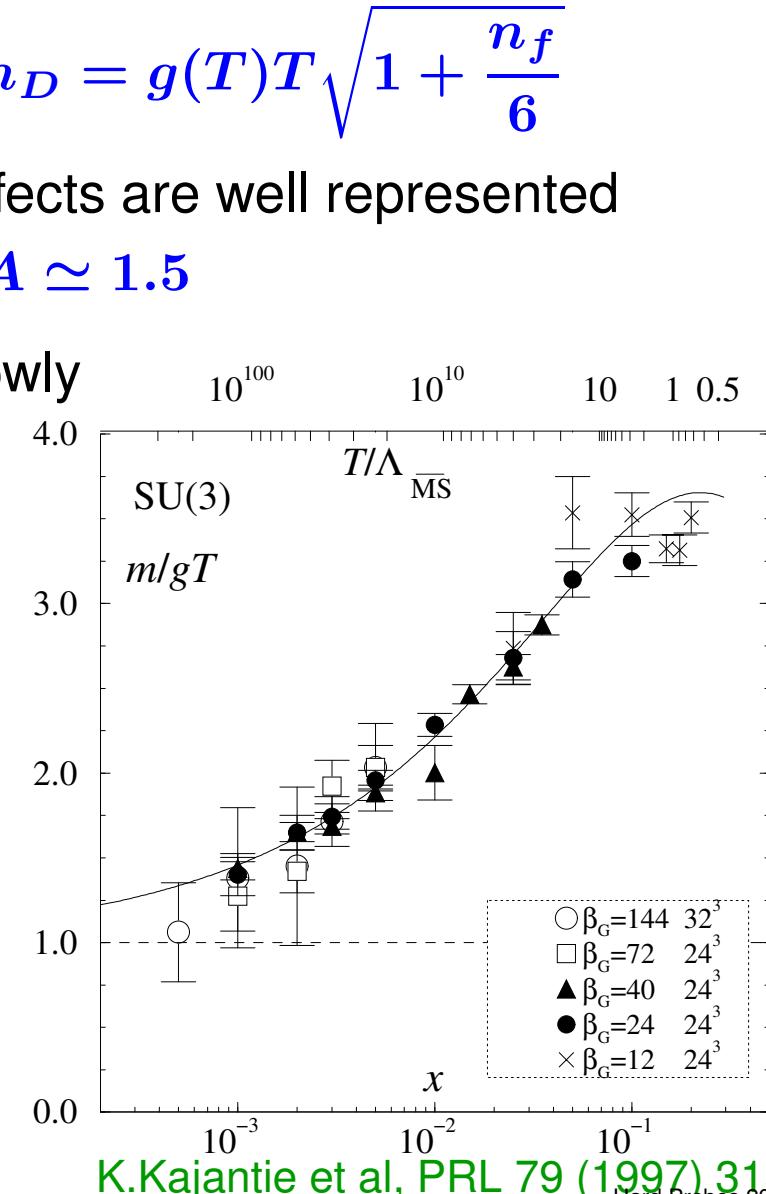
RBC-Bielefeld, preliminary

Non-perturbative Debye screening

- leading order perturbation theory: $m_D = g(T)T \sqrt{1 + \frac{n_f}{6}}$
- $T_c < T \lesssim 10T_c$: non-perturbative effects are well represented by an "A-factor": $m_D \equiv Ag(T)T$, $A \simeq 1.5$
- perturbative limit is reached very slowly
(logarithms at work!!)



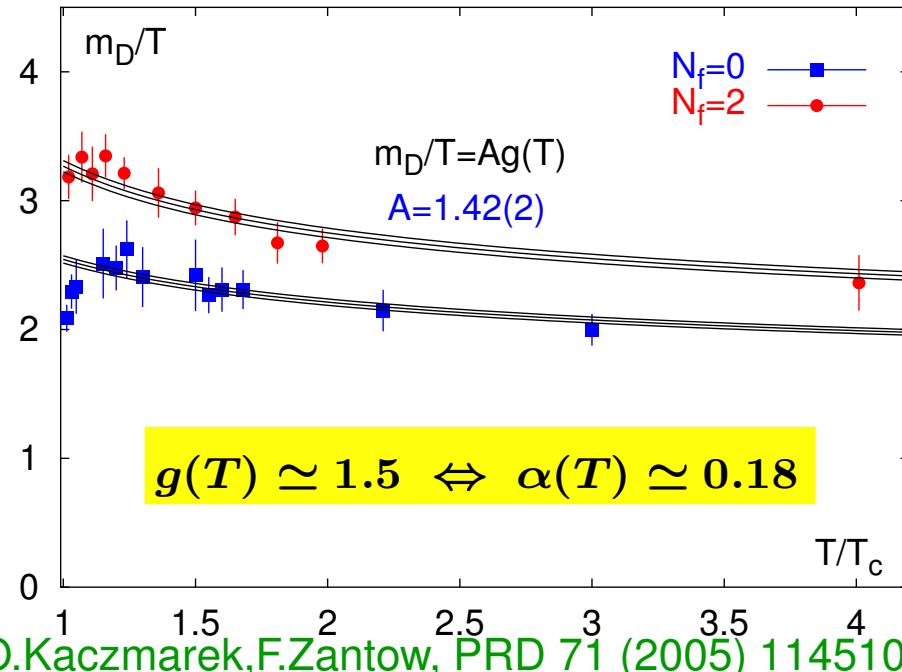
O.Kaczmarek,F.Zantow, PRD 71 (2005) 114510



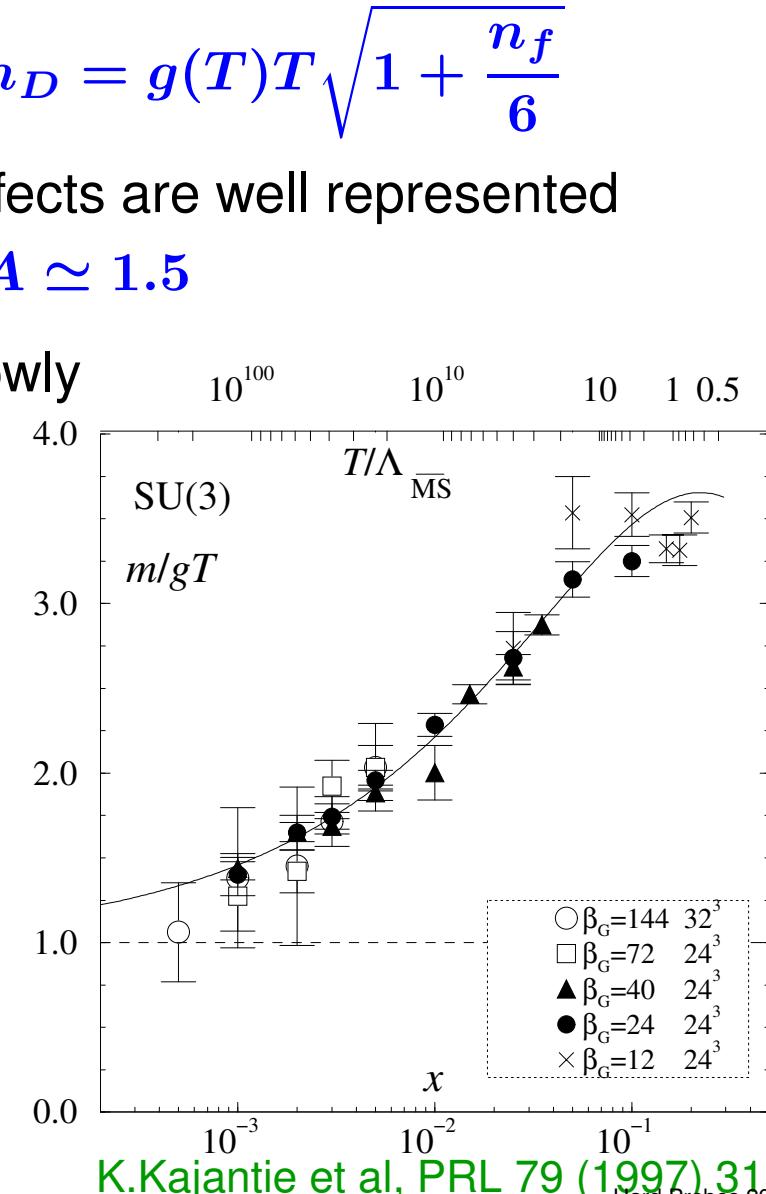
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Hard Probes 2006 – p.6/31

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Non-perturbative Debye screening μ_q -dependence

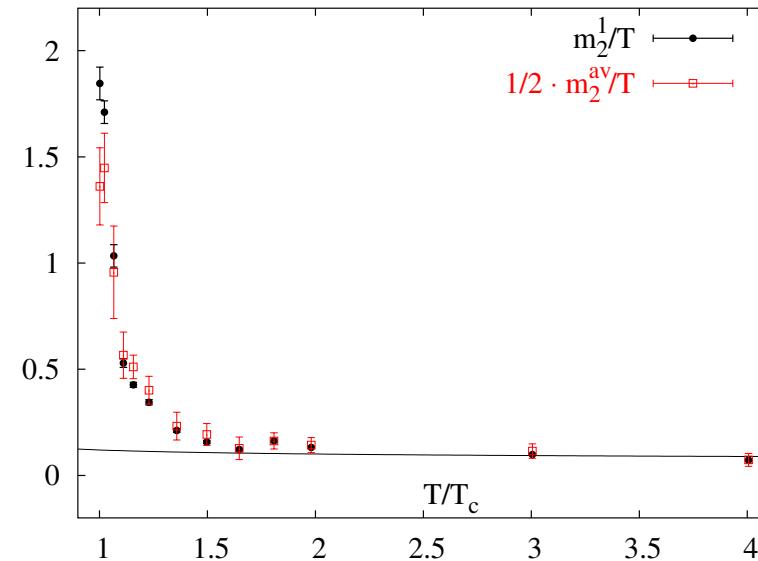
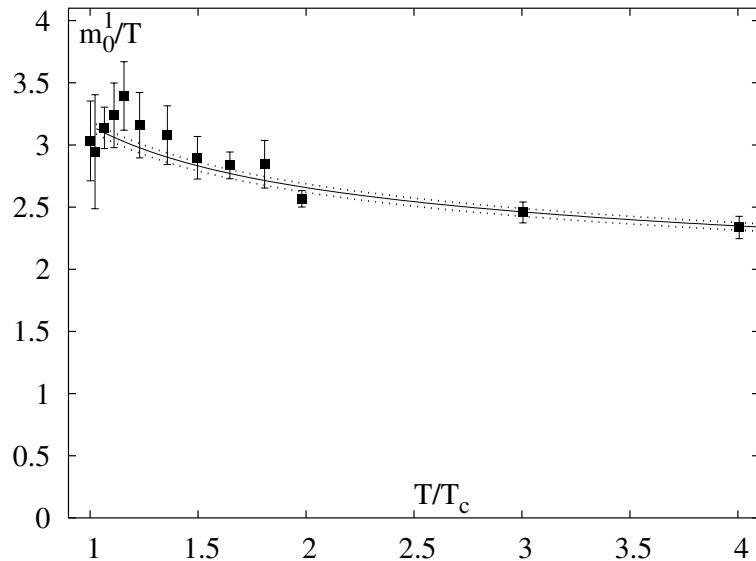
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$$m_D = g(T)T \sqrt{1 + \frac{n_f}{6} + \frac{n_f}{2\pi^2} \left(\frac{\mu_q}{T}\right)^2}$$

- Taylor expansion, 2-flavor QCD:

$$m_D(T) = m_0(T) + m_2(T) \left(\frac{\mu_q}{T}\right)^2 + \mathcal{O}(\mu_q^4)$$

$m_2(T)$: agrees with perturbation theory for $T \gtrsim 1.5 T_c$



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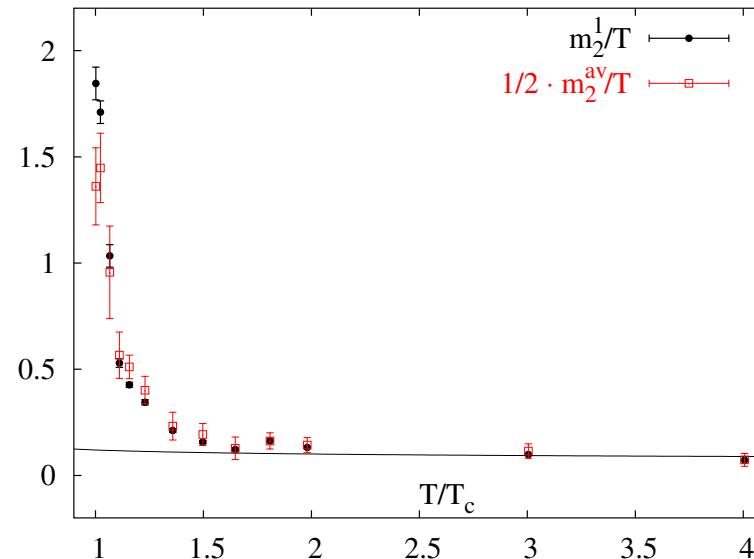
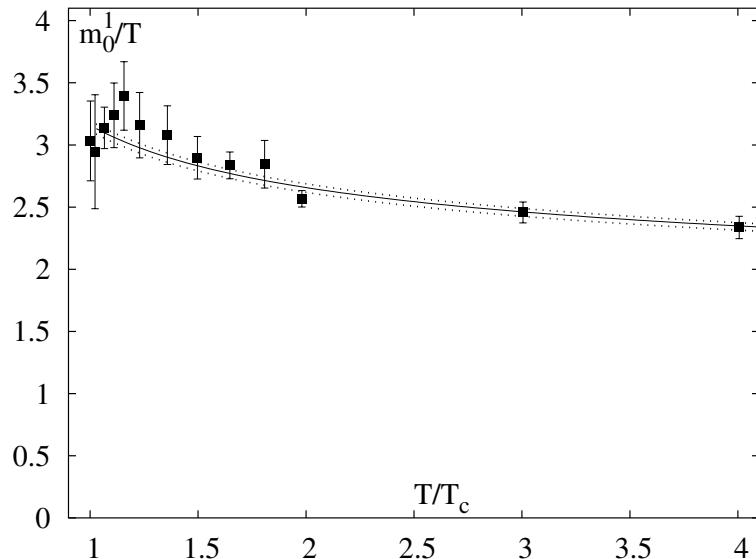
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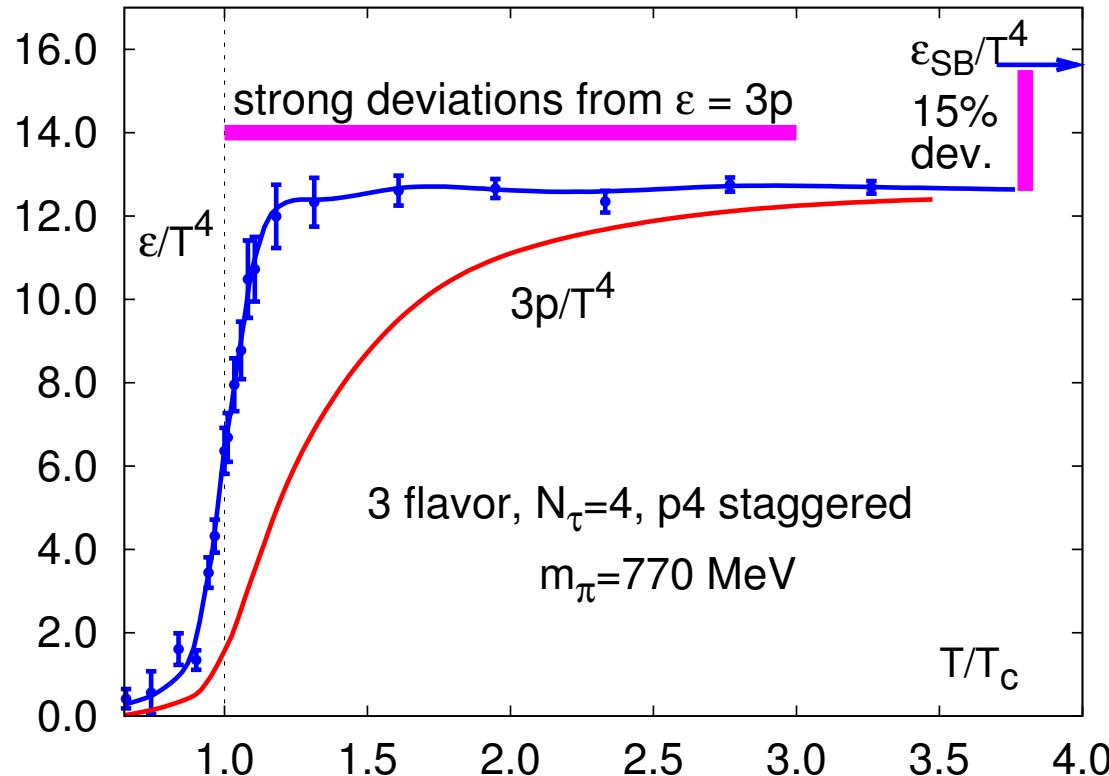
$\mathbf{m}_2(\mathbf{T})$: agrees with perturbation theory for $T \gtrsim 1.5T_c$

non-perturbative
effects are in the glue
quark sector
"perturbative"
above $T \gtrsim 1.5T_c$?



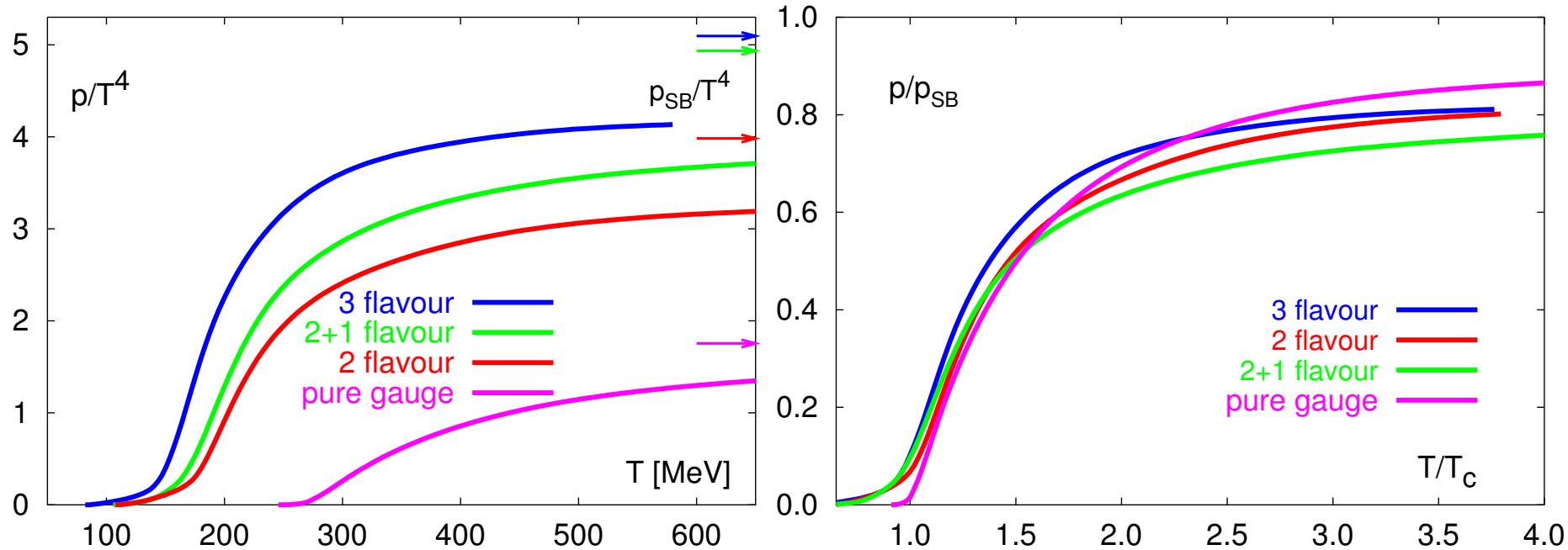
QCD equation of state

- two features of EoS are central in the ongoing discussion of the non-perturbative structure of QCD at high temperature
 - strong deviations from ideal gas behavior ($\epsilon = 3p$) for $T_c \leq T \sim 3T_c$
 - deviations from Stefan-Boltzmann limit persist even at high T

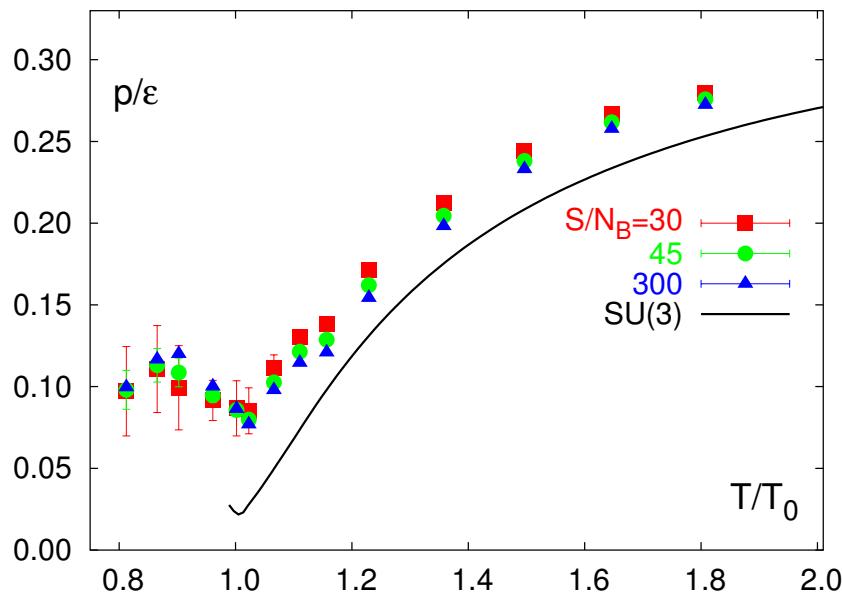


The pressure revisited

- $T \gtrsim (2\text{-}3)T_c$: deviations from ideal gas understood in terms of HTL-resummed perturbation theory
- $T \lesssim 2T_c$: strong deviations from ideal gas
- deviations from p_{SB} almost flavor independent



ISENTROPIC EQUATION OF STATE: p/ϵ



EoS for 2-flavor QCD at fixed S/N_B and EoS for SU(3) gauge theory

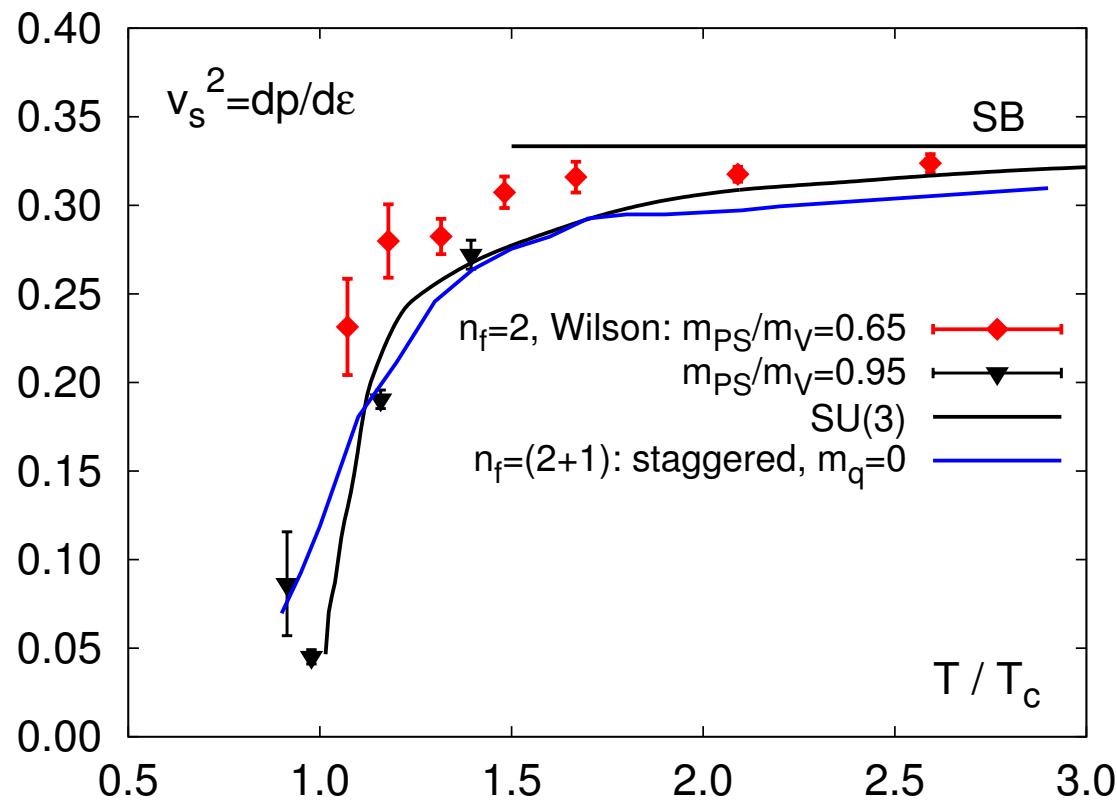
S. Ejiri et al., PRD 73 (2006) 054506

- p/ϵ vs. ϵ shows almost no dependence on S/N_B , i.e. μ_q/T
- p/ϵ has only weak dependence on n_f (cut-off effects??)
- phenomenological EoS for $T_0 \lesssim T \lesssim 2T_0$

$$\frac{p}{\epsilon} = \frac{1}{3} \left(1 - \frac{1.2}{1 + 0.5\epsilon} \right) , \quad \left(\frac{p}{\epsilon} \right)_{min} \simeq 0.075$$

Velocity of sound

- steep EoS:
 - rapid change of energy density; slow change of pressure
 - ⇒ reduced velocity of sound ⇒ more time for equilibration



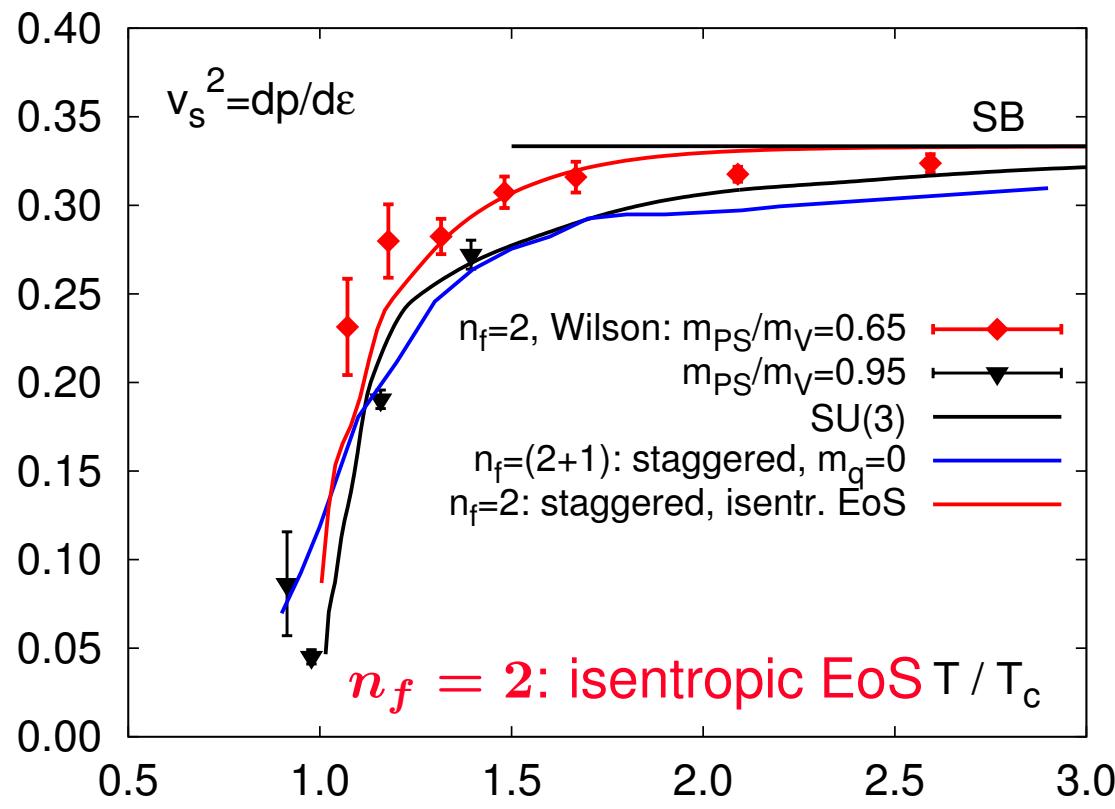
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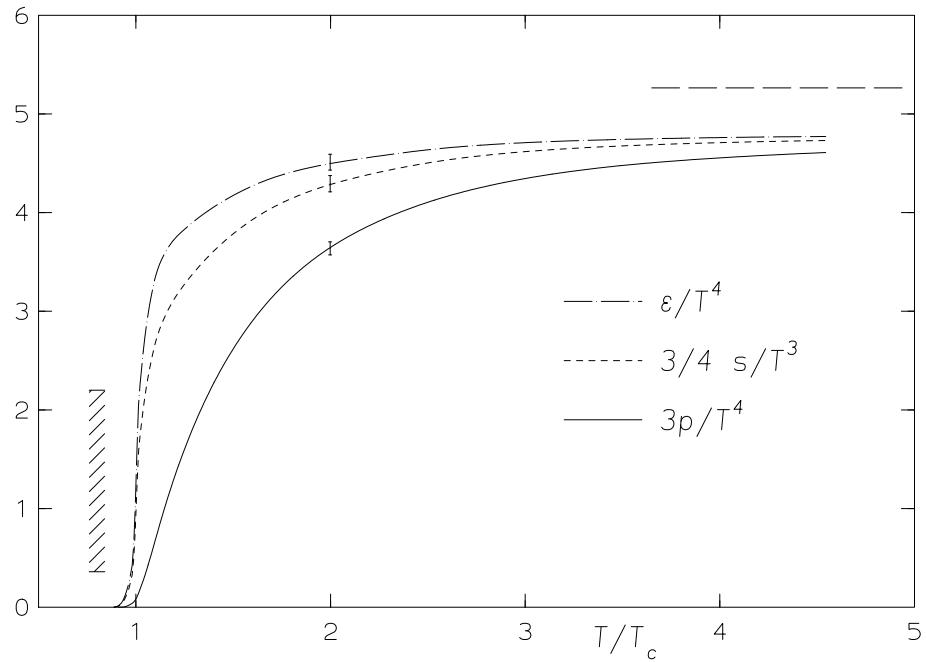
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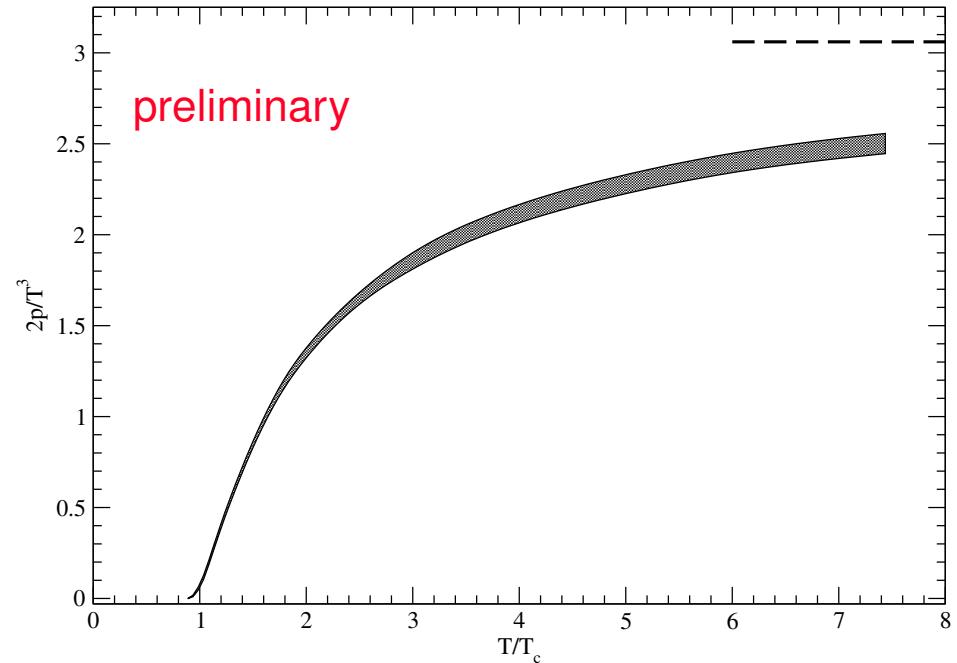
SU(3) Thermodynamics - revisited

- SU(3) EoS deviates from ideal gas by about 15% at $4T_c$
- slow approach to the high temperature limit consistent with logarithmic running of the coupling ((2+1)-d: $g_3^2 \sim g^2/T$)

(3 + 1)-d QCD: $g^2(T) \sim 1/\ln(T/\Lambda)$

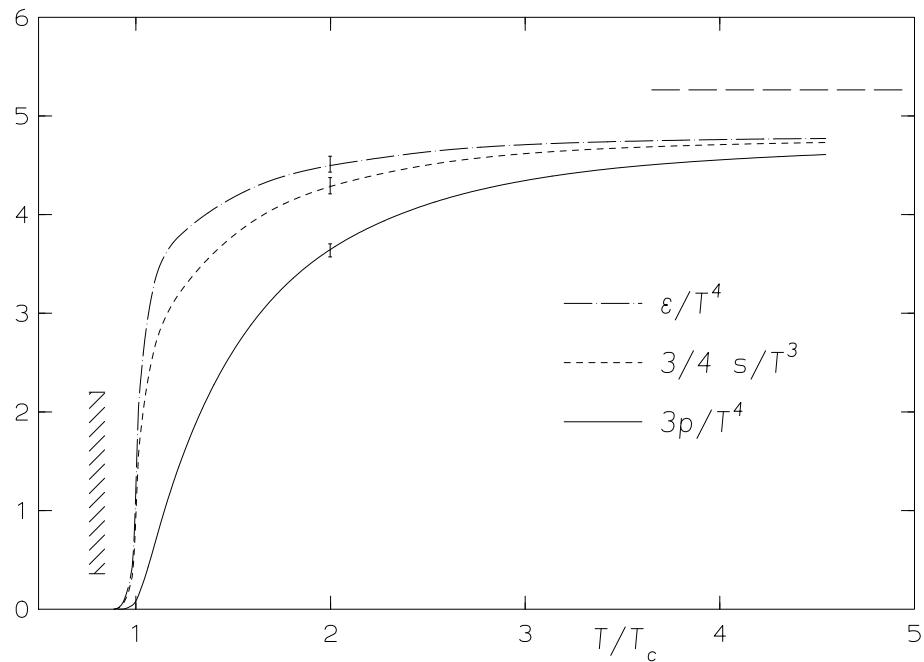


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- slow approach to the high temperature limit
- consistent with logarithmic running of the coupling (cf. 4d vs. 3d)



~ 15% deviations from ideal gas
NOTE: p , ϵ , s normalized to be zero
at $T = 0$;
non-perturbative vacuum properties
show up at high-T

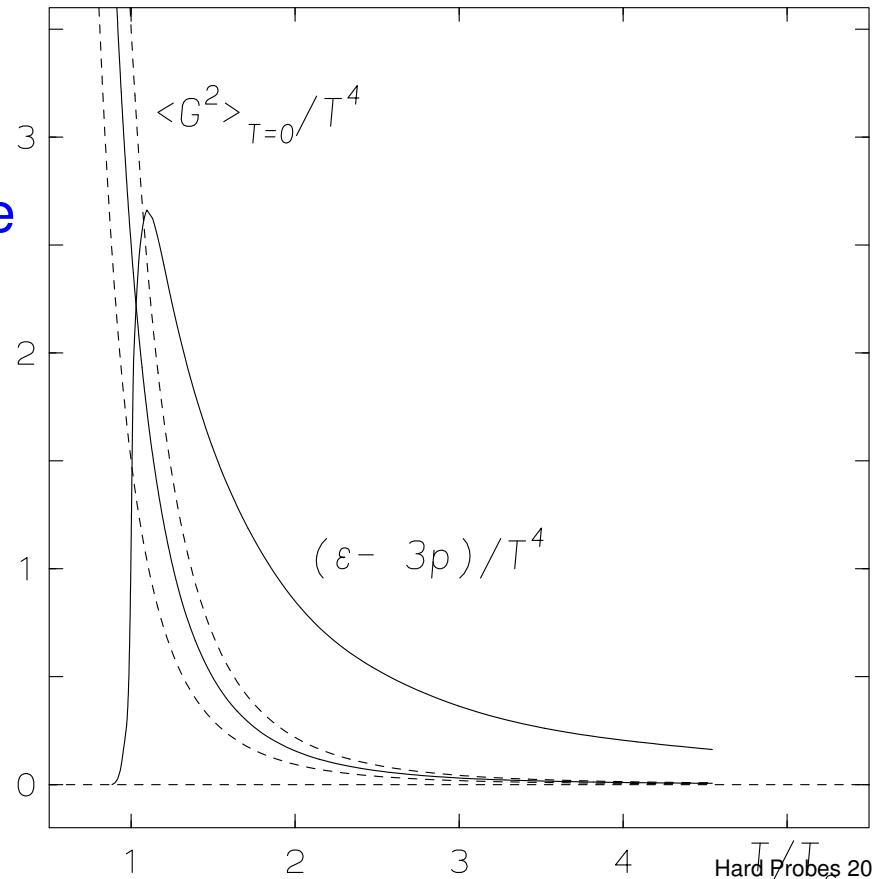
SU(3) Thermodynamics - revisited: $\langle G^2 \rangle_T$

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$T = 0$: non-vanishing gluon condensate

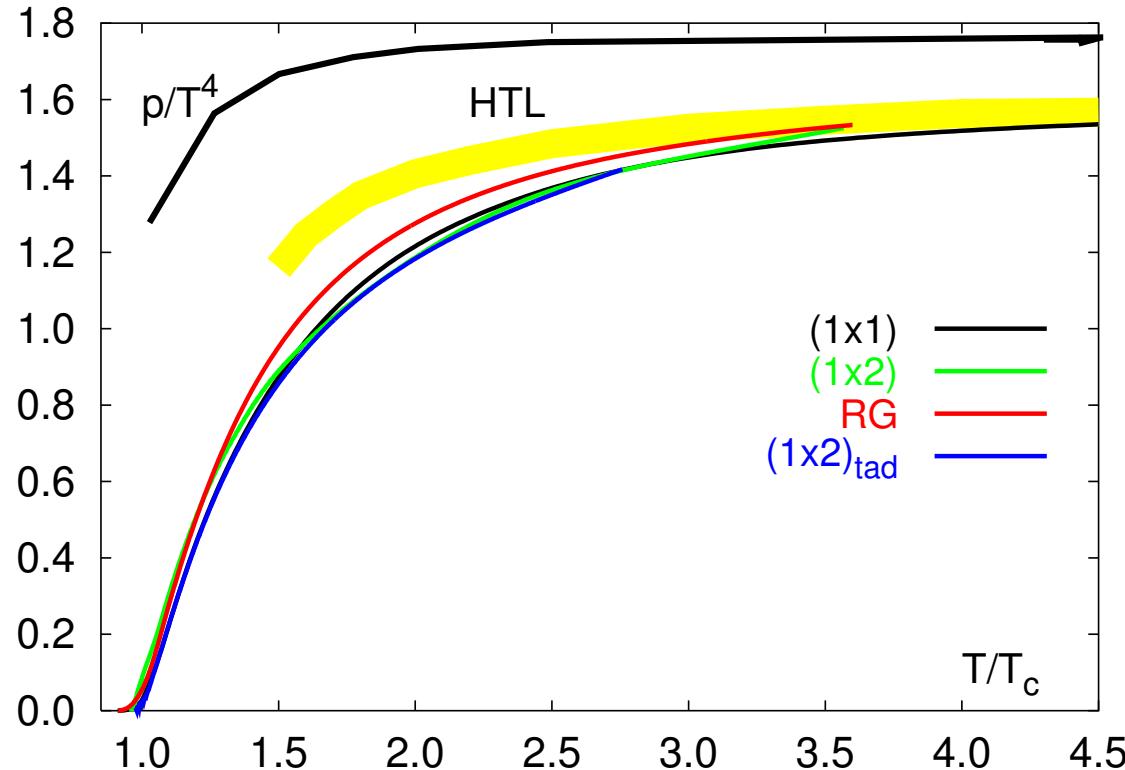
$$\epsilon - 3p = \langle G^2 \rangle_{T=0} - \langle G^2 \rangle_T$$

non-perturbative vacuum properties
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SU(3) Equation of State pressure: LGT vs. HTL

high T part of the pressure calculated on the lattice is in good agreement with HTL-resummed perturbation theory for $T \gtrsim 3T_c$



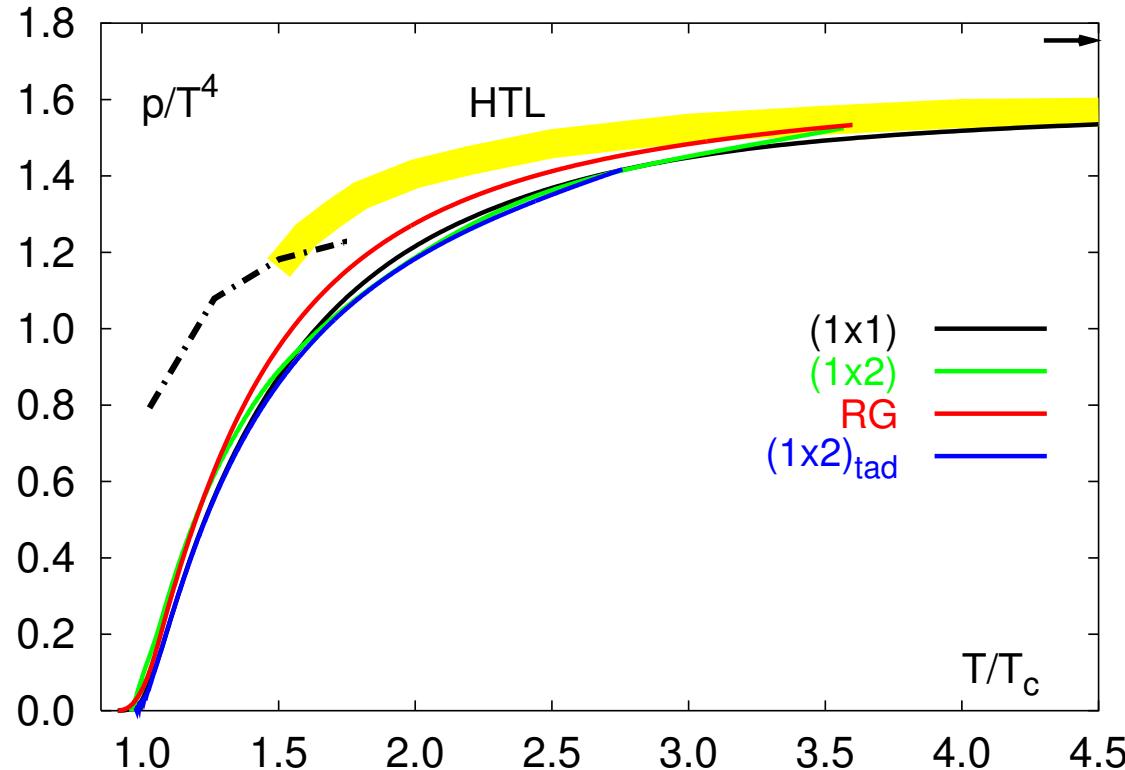
bag pressure:
 $\simeq 0.5(T_c/T)^4$

HTL: J.P. Blaizot,
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PL B470 (99) 181

bag pressure negligible for $T > 2T_c$,
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Screening of heavy quark free energies – remnant of confinement above T_c –

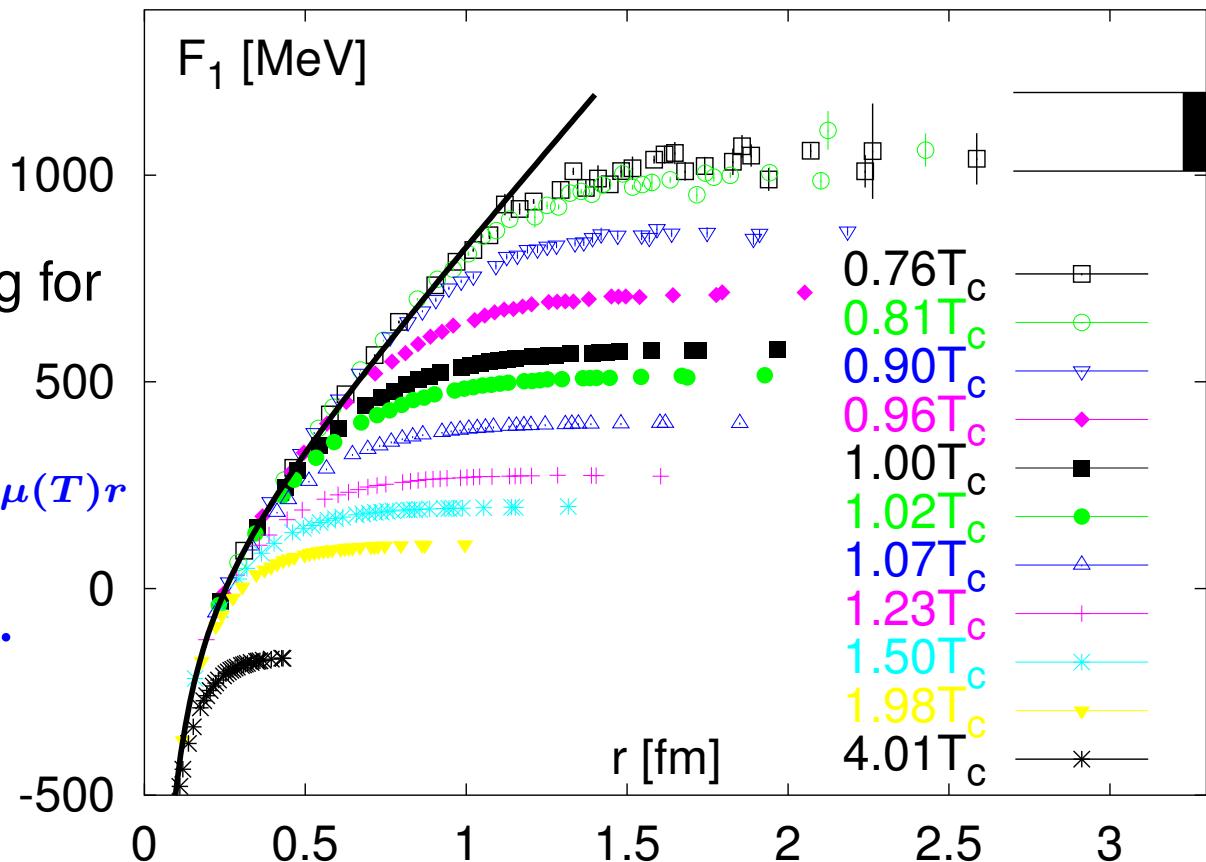
pure gauge: O.Kaczmarek, FK, P. Petreczky, F. Zantow, PRD70 (2005) 074505

2-flavor QCD: O.Kaczmarek, F. Zantow, Phys. Rev. D71 (2005) 114510

- singlet free energy

- $T \simeq T_c$: screening for $r \gtrsim 0.5$ fm

$$F_1(r, T) \sim \frac{\alpha(T)}{r} e^{-\mu(T)r} + \text{const.}$$



- $F_1(r, T)$ follows linear rise of $V_{\bar{q}q}(r, T = 0) = -\frac{4\alpha(r, T = 0)}{3r} + \sigma r$ for $T \lesssim 1.5T_c$, $r \lesssim 0.3$ fm

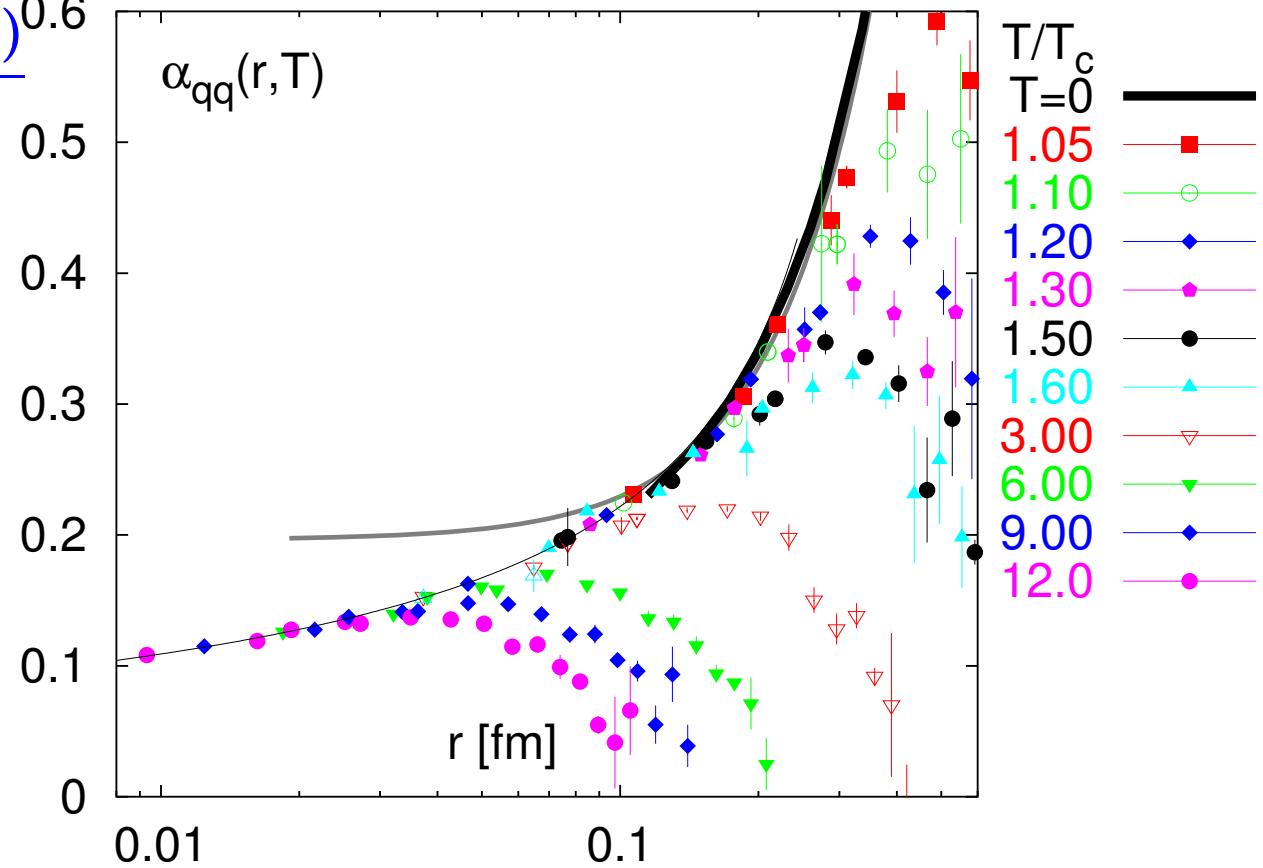
Singlet free energy and asymptotic freedom

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- singlet free energy defines a running coupling:

$$\alpha_{\text{eff}} = \frac{3r^2}{4} \left(\frac{dF_1(r, T)}{dr} \right)^{0.6}$$



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large distance: constant

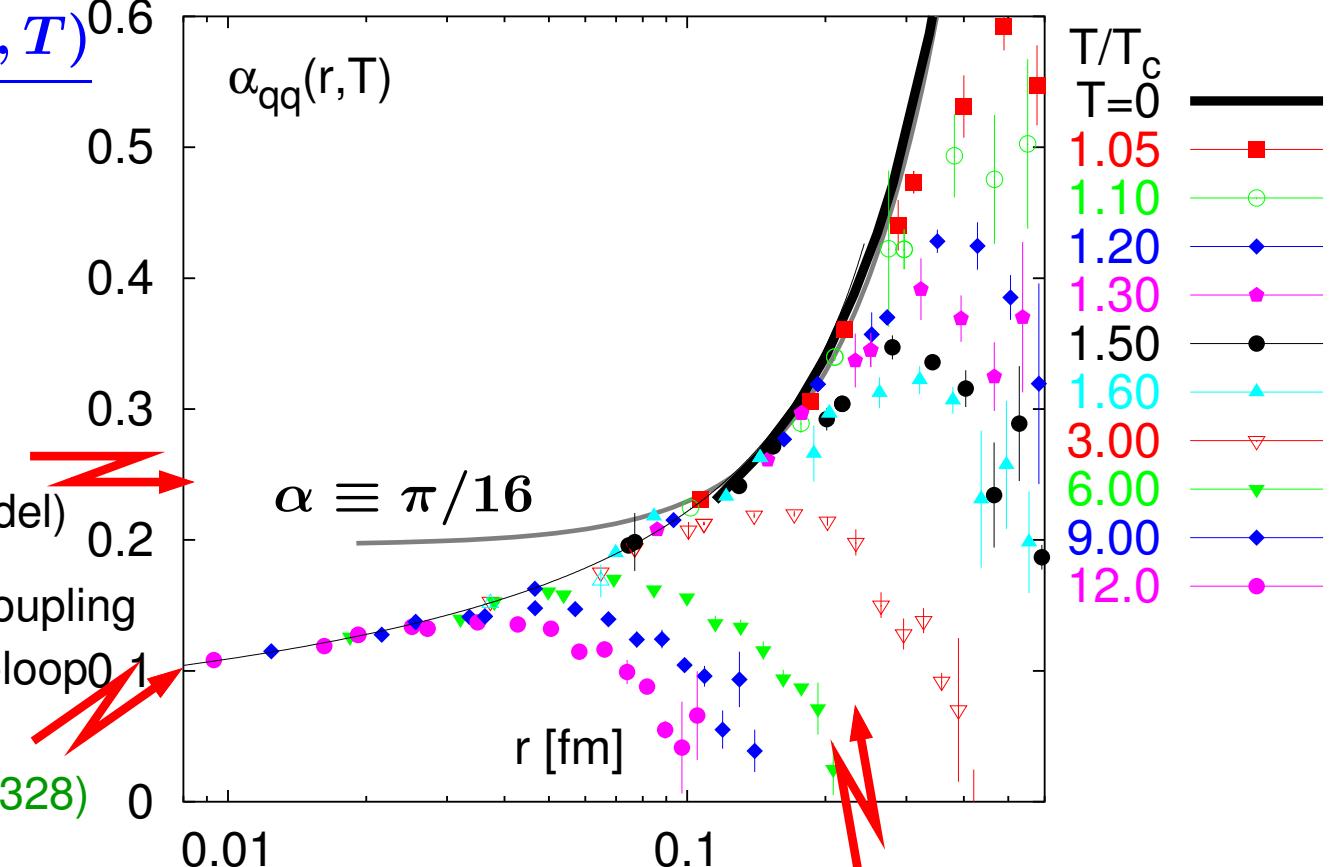
Coulomb term (string model)

short distance: running coupling

$\alpha(r)$ from ($T = 0$), 3-loop

(S. Necco, R. Sommer,

Nucl. Phys. B622 (2002) 328



- short distance physics \Leftrightarrow vacuum physics

T-dependence starts in non-perturbative regime for $T \lesssim 3 T_c$

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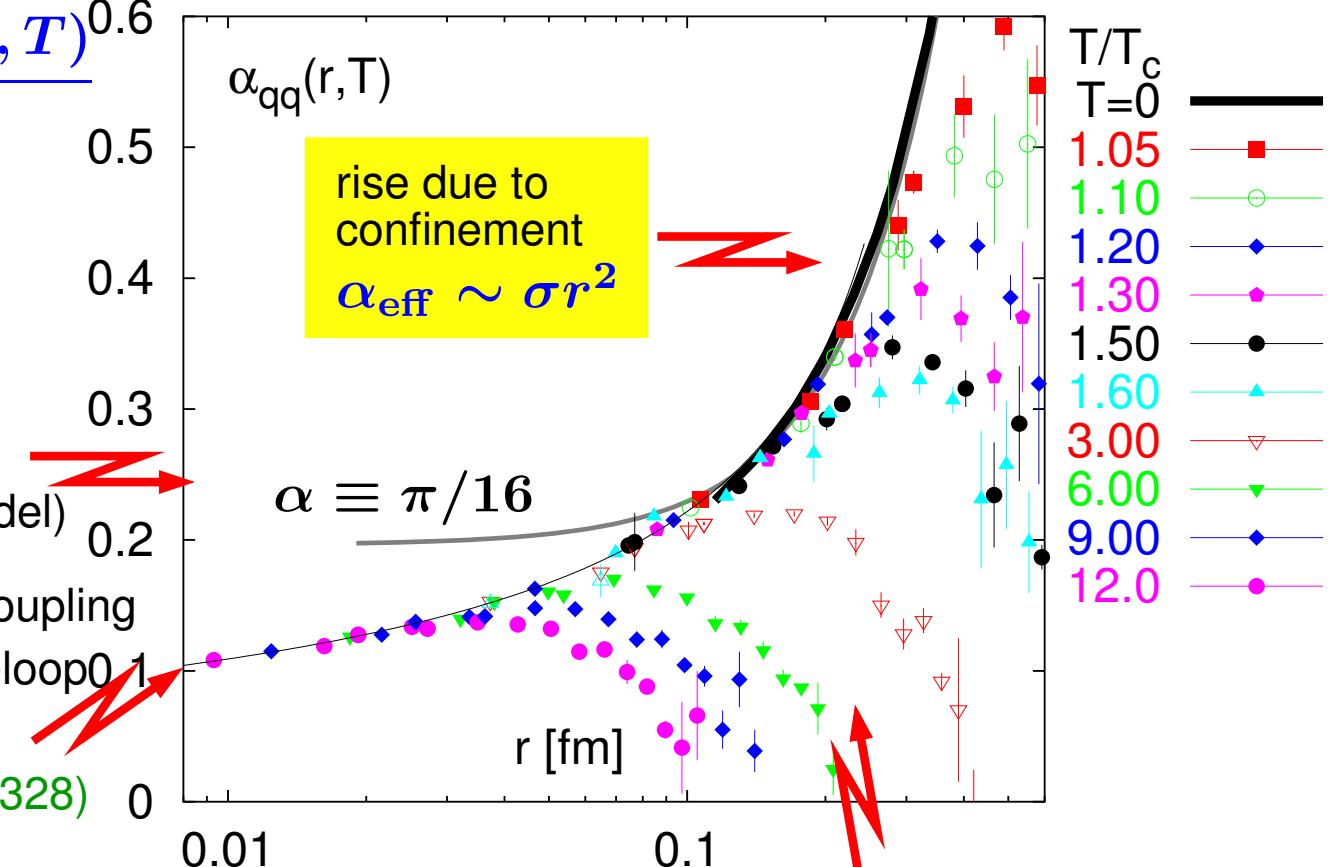
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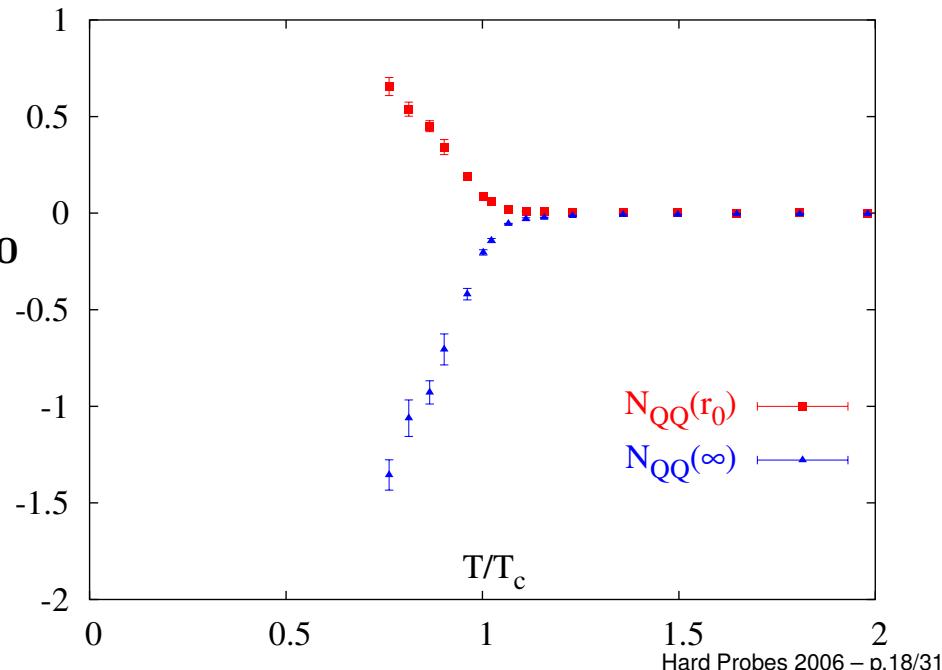
String breaking and screening

Does a heavy quark bind a light (anti) quark?

- Static quark-quark source in a thermal heat bath
 - triality = 0: medium provides additional quark or 2 anti-quarks
- average quark number in the presence of two static quark sources

$$Z_{QQ}(T, \mu, r) = \int dU \text{Tr} L_0 \text{Tr} L_r \det D(m_q, \mu) e^{-\beta S_G}$$

$$N_{QQ}(T, r) = \frac{\partial \ln Z_{qq}(T, \mu, r)}{\partial \mu/T} \Big|_{\mu=0}$$



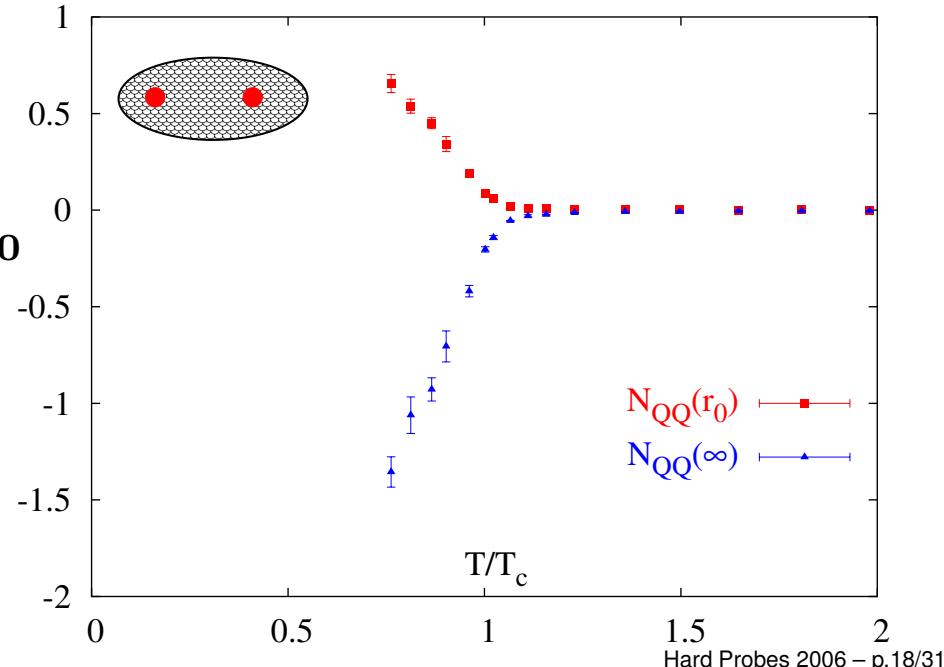
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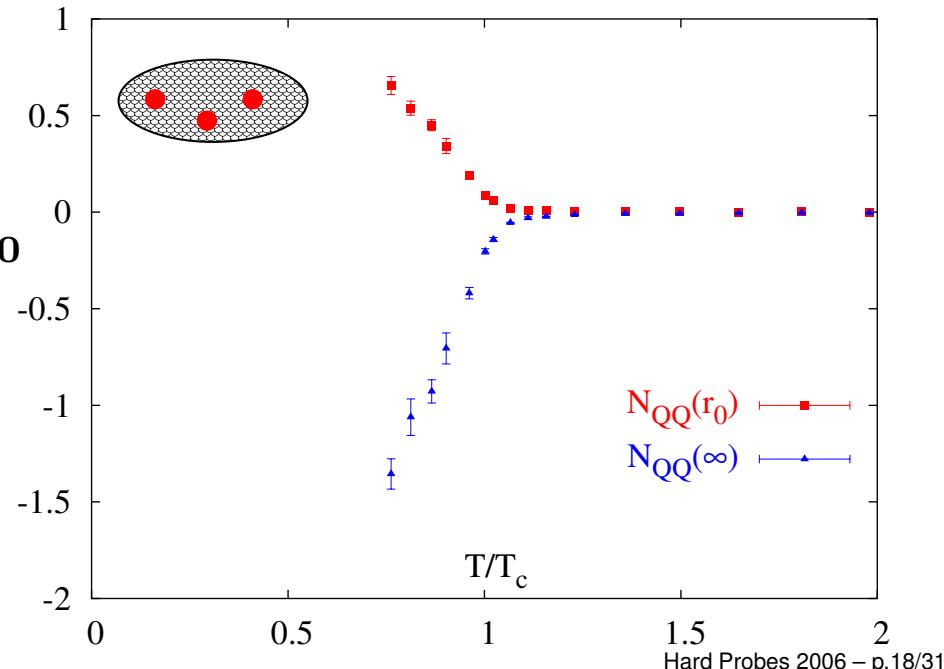
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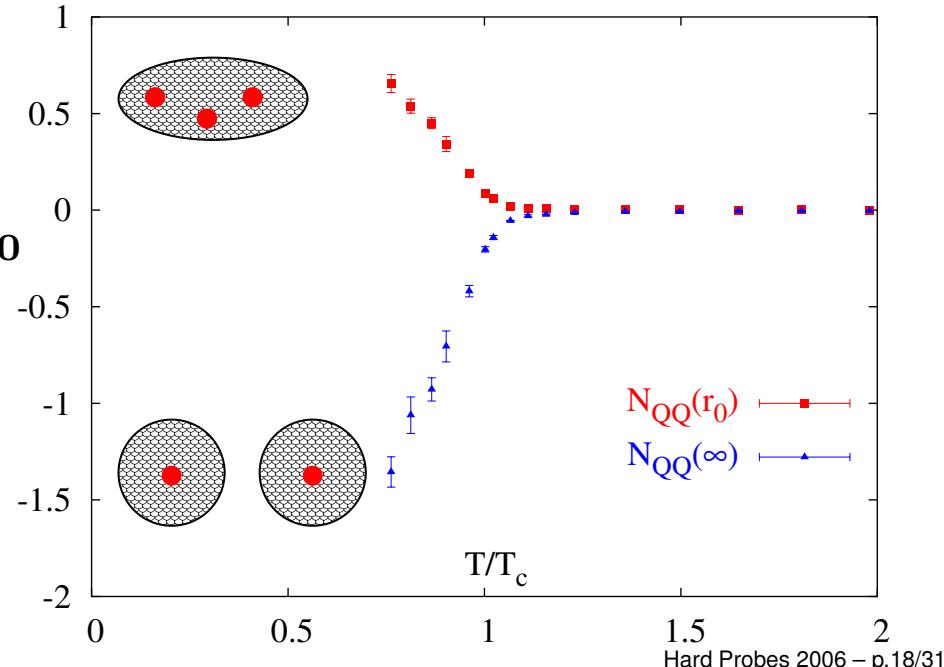
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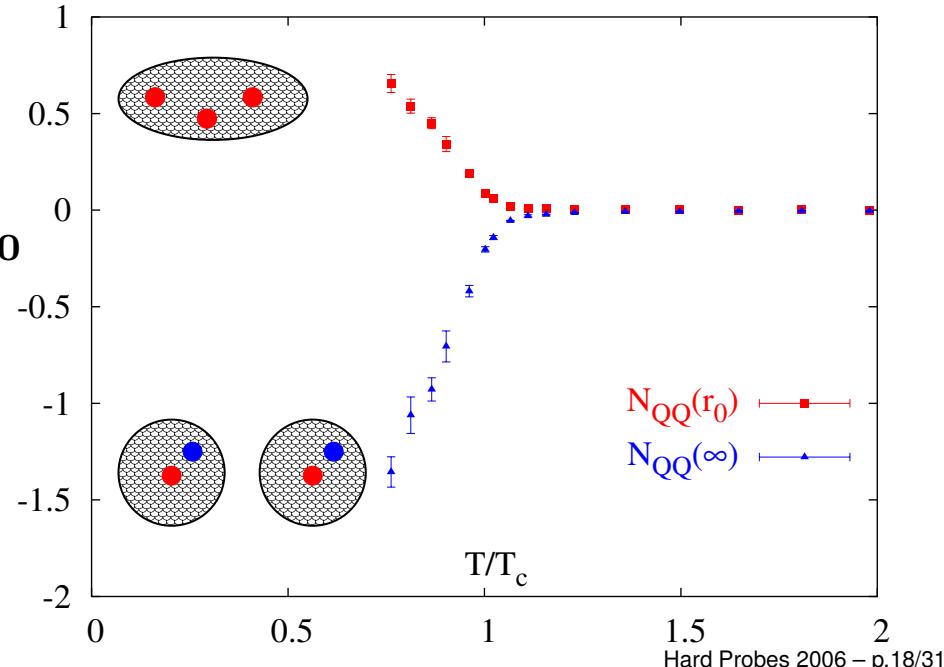
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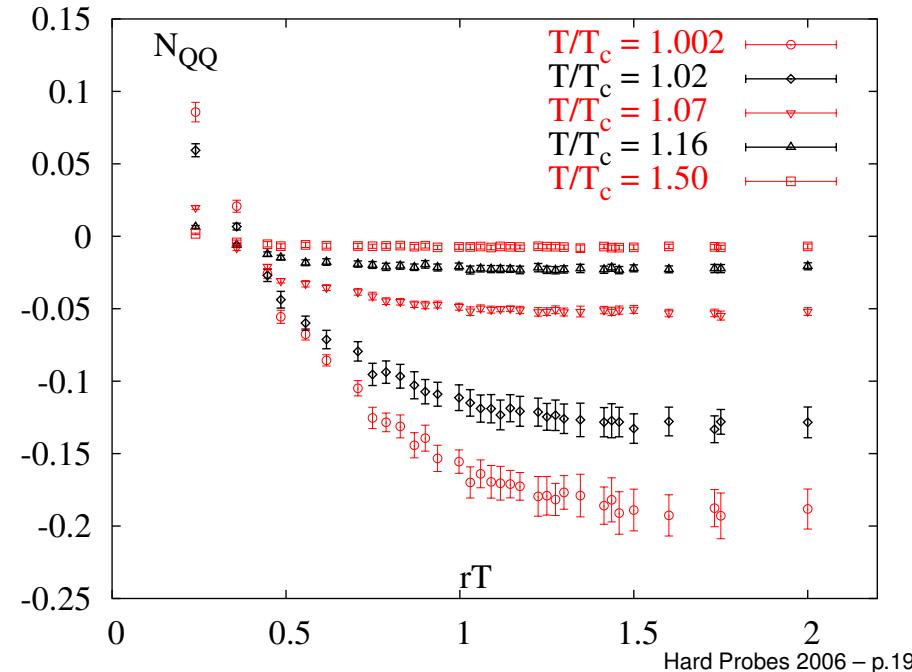
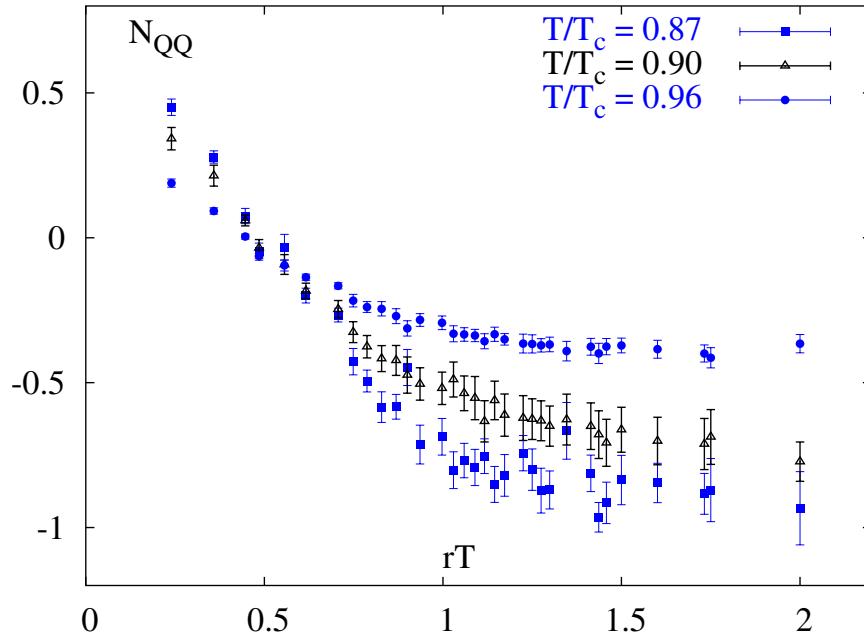
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String breaking and screening

Does a heavy quark bind a light (anti) quark?

- $N_{QQ}(r, T)$ depends on separation between static quark-quark source
- $r = r_{b/s} \simeq 0.5/T$: screening changes from q -dominated to $\bar{q}\bar{q}$ -dominated
- $T \gtrsim 1.1T_c$: presence of q or $\bar{q}\bar{q}$ not important for screening



Screening of heavy quark free energies – remnant of confinement above T_c –

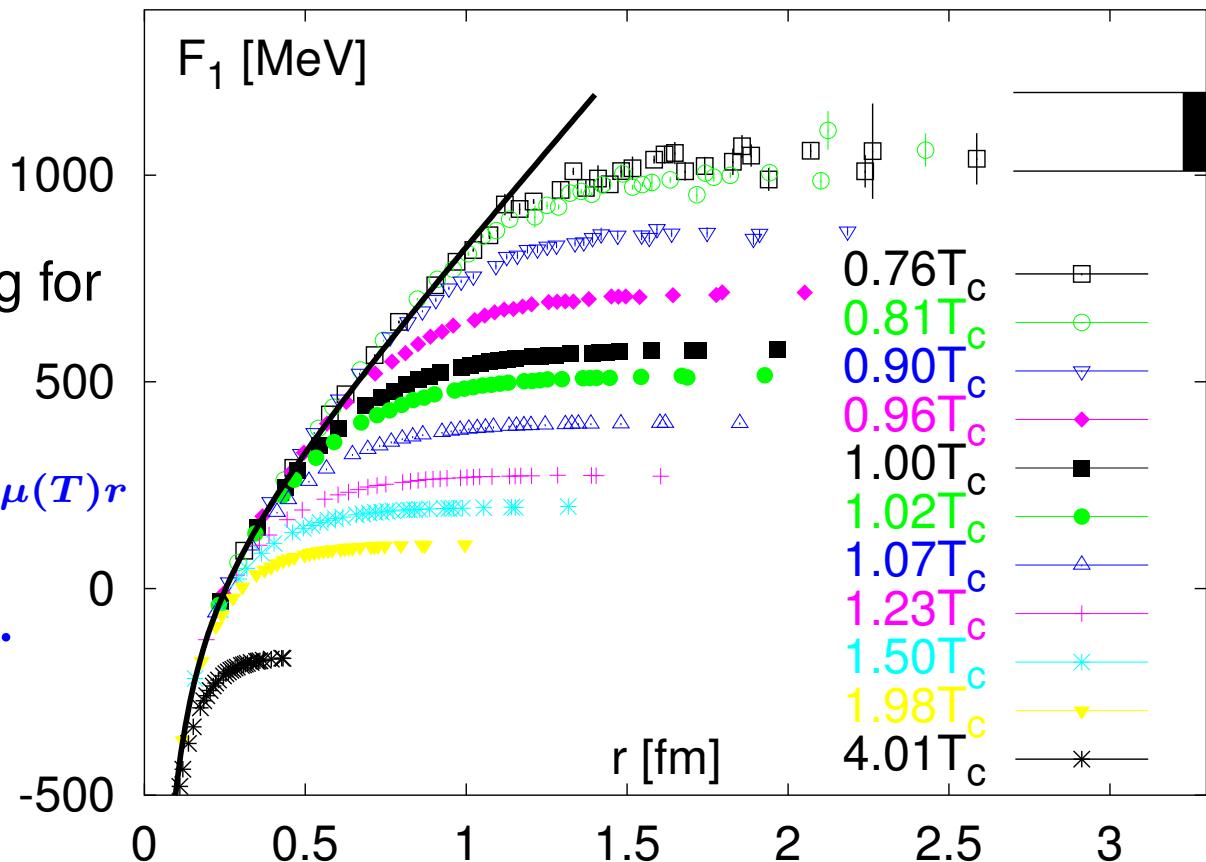
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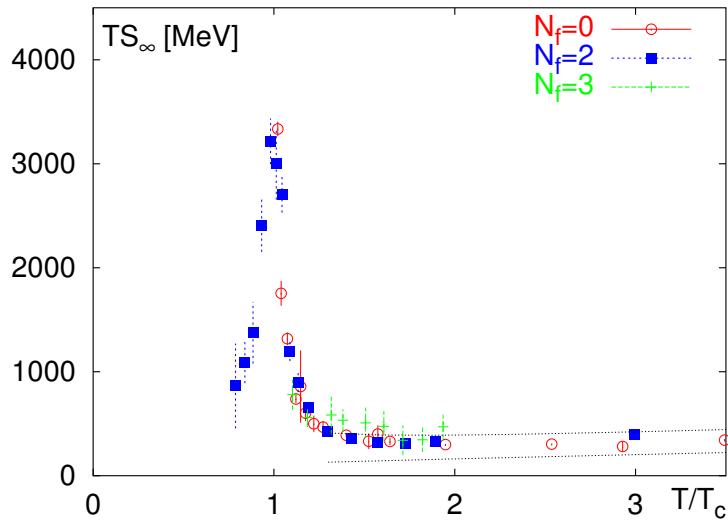
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Screening of heavy quark free energies at large distance

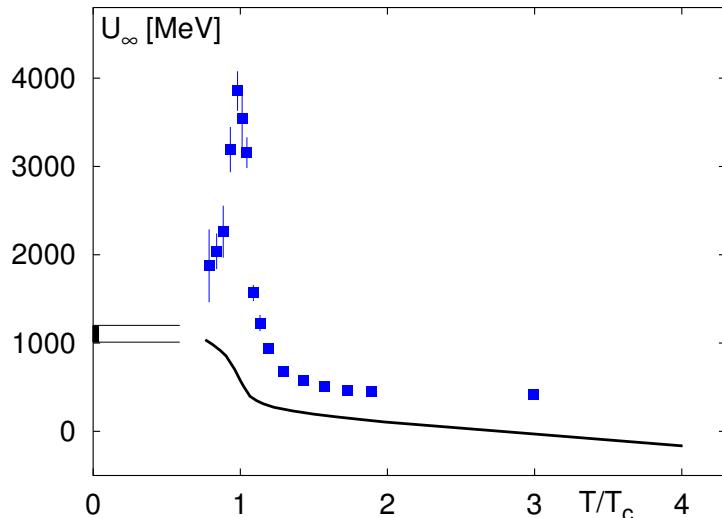


Excess entropy at $r \rightarrow \infty$

It's all in the glue:

$$T \lesssim T_c: S_{\bar{q}q}^{nf=2}(\infty, T) \simeq S_{\bar{q}q}^{nf=0}(\infty, T)$$

$$\Delta(\text{Entropy})/\text{Quark} \sim 15$$



Energy needed to screen 2 quarks

Large increase of energy close to T_c

Why not simply create another $\bar{q}q$ pair?

large entropy in the glue rearrangement
compensates for higher energy!!

Hadronic fluctuations at $\mu_q = 0$ from Taylor expansion coefficients for $\mu_q > 0$

V. Koch, A. Majumder, J. Randrup, PRL 95 (2005) 182301

S. Ejiri, FK, K. Redlich, PLB633 (2006) 275

- quark number and isospin chemical potentials:

$$\mu_q = \frac{1}{2}(\mu_u + \mu_d), \quad \mu_I = \frac{1}{2}(\mu_u - \mu_d)$$

- expansion coefficients evaluated at $\mu_{q,I} = 0$ are related to hadronic fluctuations at $\mu = 0$:

↑ baryon number, isospin, charge

event-by-event fluctuations at RHIC and LHC

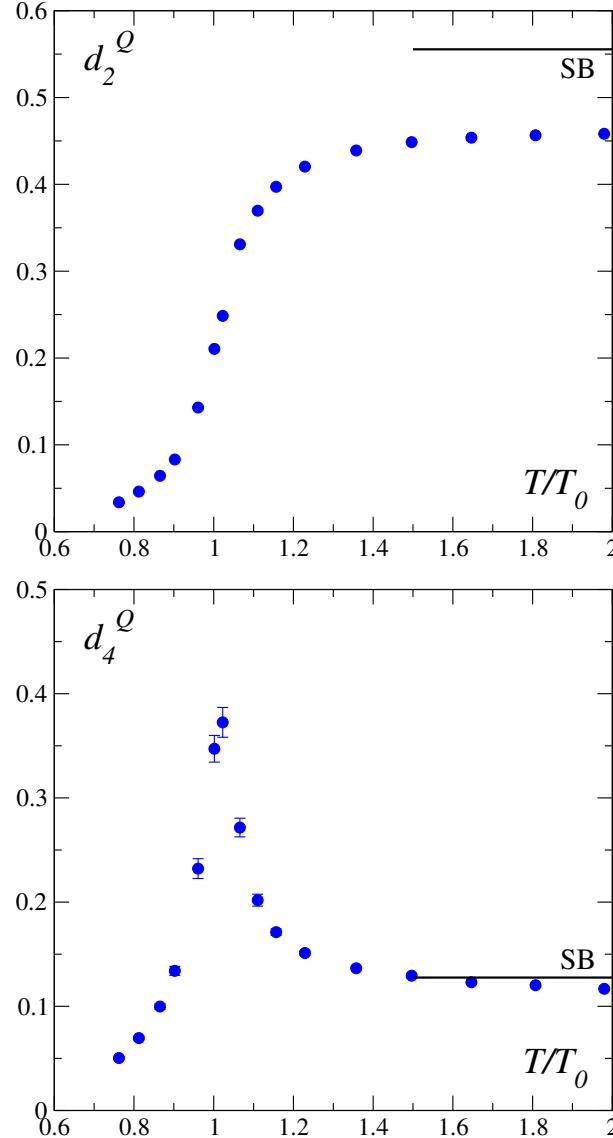
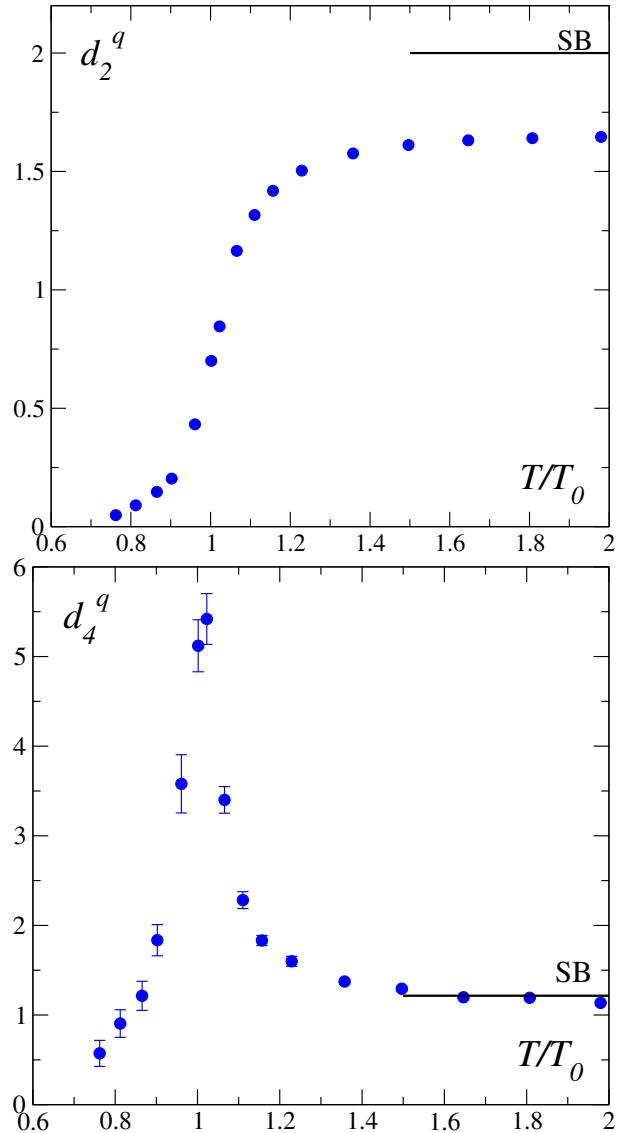
$$d_2^x = \frac{\partial^2 \ln Z}{\partial(\mu_x/T)^2} = \frac{1}{VT^3} \langle (\delta N_x)^2 \rangle_{\mu=0} = \frac{1}{VT^3} \langle N_x^2 \rangle_{\mu=0}$$

$$d_4^x = \frac{\partial^4 \ln Z}{\partial(\mu_x/T)^4} = \frac{1}{VT^3} (\langle (\delta N_x)^4 \rangle - 3 \langle (\delta N_x)^2 \rangle)_{\mu=0} = \frac{1}{VT^3} (\langle N_x^4 \rangle - 3 \langle N_x^2 \rangle)_{\mu=0}$$

with , $x = q, I, Q$ and $\partial_Q \equiv \frac{2}{3} \frac{\partial}{\partial \mu_u/T} - \frac{1}{3} \frac{\partial}{\partial \mu_d/T}$

Quark number and charge fluctuations at $\mu_B = 0$; 2-flavor QCD ($m_\pi \simeq 770 \text{ MeV}$)

C. Allton et al. (Bielefeld-Swansea), PRD71 (2005) 054508



monotonic increase;
close to ideal
gas value for
 $T \gtrsim 1.5T_c$

develops cusp
at T_c

reaches ideal
gas value for
 $T \gtrsim 1.5T_c$

Hadronic fluctuations and chiral symmetry restoration

- expect 2^{nd} order transition in 3-d, O(4) symmetry class;

$$\text{scaling field: } t = \left| \frac{T - T_c}{T_c} \right| + A \left(\frac{\mu_q}{T_c} \right)^2 , \quad \mu_{crit} = 0$$

$$\text{singular part: } f_s(T, \mu_u, \mu_d) = b^{-1} f_s(t b^{1/(2-\alpha)}) \sim t^{2-\alpha}$$

$$\frac{\partial^2 \ln \mathcal{Z}}{\partial \mu_q^2} \sim t^{1-\alpha} \quad , \quad \frac{\partial^4 \ln \mathcal{Z}}{\partial \mu_q^4} \sim t^{-\alpha} \quad (\mu = 0)$$

- O(4)/O(2): $\alpha < 0$, small \Rightarrow

$\langle (\delta N_q)^2 \rangle$ dominated by T-dependence of regular part

$\langle (\delta N_q)^4 \rangle$ develops a cusp

Quark number in Boltzmann approximation

$$\begin{aligned} p_m/T^4 &= F(T, m, V) \cosh(\textcolor{red}{B}\mu_q/T) \\ d_2^q &\equiv \frac{\partial^2 p_m/T^4}{\partial(\mu_q/T)^2} = \textcolor{red}{B}^2 F(T, m, V) \cosh(\textcolor{red}{B}) \\ d_4^q &\equiv \frac{\partial^4 p_m/T^4}{\partial(\mu_q/T)^4} = \textcolor{red}{B}^4 F(T, m, V) \cosh(\textcolor{red}{B}) \end{aligned}$$

ratio of fourth (d_4^q) and second (d_2^q) cumulant of quark number fluctuation gives "unit of charge" carried by the particle with mass " m ":

$$m \gg T \quad \Rightarrow \quad R_{4,2}^q \equiv \frac{d_4^q}{d_2^q} = \textcolor{blue}{B}^2$$

Charge fluctuations in Boltzmann approximation

- hadronic resonance gas: contributions from isosinglet ($G^{(1)} : \eta, \dots$) and isotriplet ($G^{(3)} : \pi, \dots$) mesons as well as isodoublet ($F^{(2)} : p, n, \dots$) and isoquartet ($F^{(4)} : \Delta, \dots$) baryons

$$\begin{aligned}\frac{p(T, \mu_q, \mu_I)}{T^4} &\simeq G^{(1)}(T) + G^{(3)}(T) \frac{1}{3} \left(2 \cosh \left(\frac{2\mu_I}{T} \right) + 1 \right) \\ &\quad + F^{(2)}(T) \cosh \left(\frac{3\mu_q}{T} \right) \cosh \left(\frac{\mu_I}{T} \right) \\ &\quad + F^{(4)}(T) \frac{1}{2} \cosh \left(\frac{3\mu_q}{T} \right) \left[\cosh \left(\frac{\mu_I}{T} \right) + \cosh \left(\frac{3\mu_I}{T} \right) \right]\end{aligned}$$

- charge fluctuations at $\mu_q = \mu_I = 0$;
isospin quartet $F^{(4)}$ contains baryons carrying charge 2

$$R_{4,2}^Q \equiv \frac{d_4^Q}{d_2^Q} = \frac{4G^{(3)} + 3F^{(2)} + 27F^{(4)}}{4G^{(3)} + 3F^{(2)} + 9F^{(4)}} \rightarrow 1 \text{ for } T \rightarrow 0$$

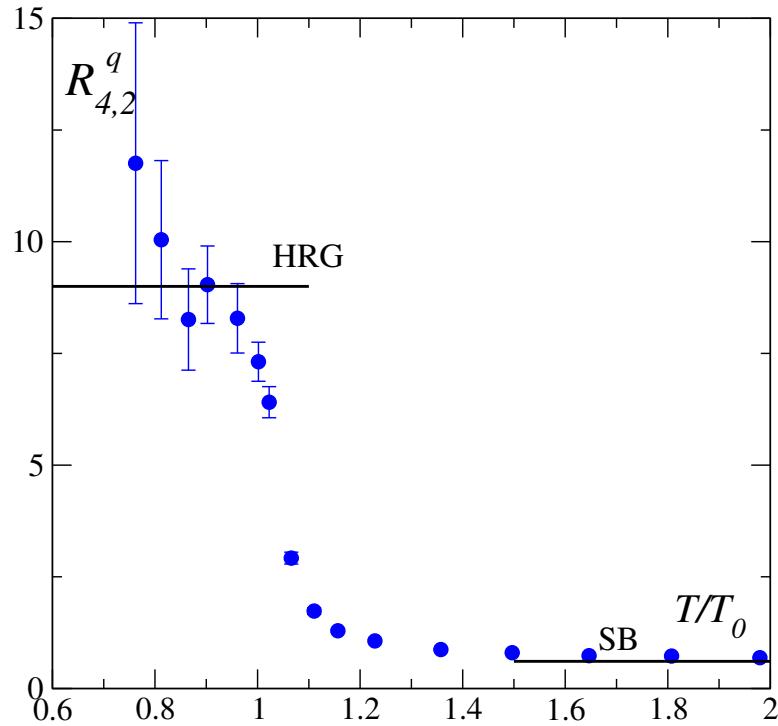
contribution of doubly charged baryons increases quartic relative to quadratic fluctuations

Cumulant ratios

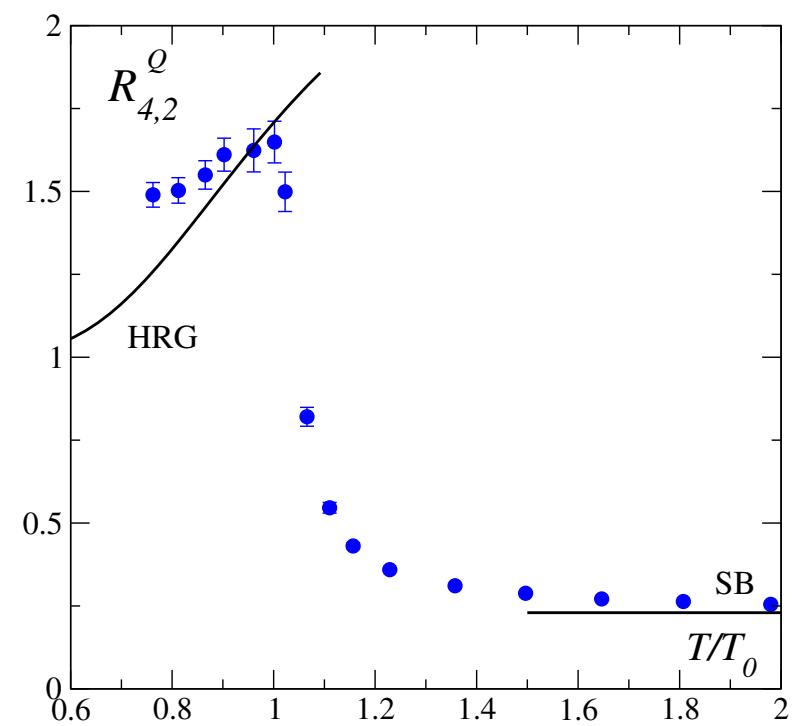
- ratios of cumulants reflect carriers of baryon number and charge

$$R_{4,2}^x = d_4^x / d_2^x \quad , \quad x = q, Q$$

$$R_{4,2}^q = \begin{cases} \frac{9}{\pi^2} & , \text{HRG} \\ \frac{6}{\pi^2} + \mathcal{O}(g^3) & , \text{high} - T \end{cases}$$



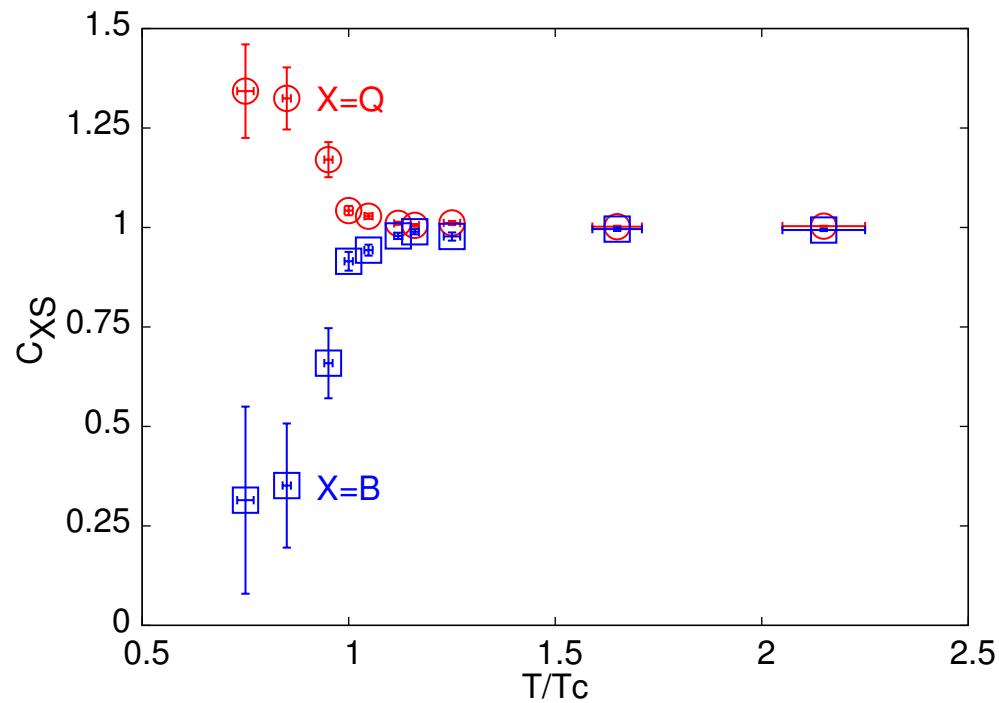
$$R_{4,2}^Q = \begin{cases} \frac{1}{34} & , \text{HRG}, T \rightarrow 0 \\ \frac{34}{15\pi^2} + \mathcal{O}(g^3) & , \text{high} - T \end{cases}$$



Off-diagonal correlations

- similar: correlations between eg. strangeness and baryon number sensitive to "carriers of quantum numbers"

$$\chi_{XS} \equiv \langle XS \rangle - \langle X \rangle \langle S \rangle , \quad X = B, Q$$



R.V. Gavai, S. Gupta, PRD 73 (2006) 014004

inspired by: V. Koch, A. Majumder, J. Randrup, PRL 95 (2005) 182301

Conclusions

- glue sticks

the interesting non-perturbative physics in QCD happens in the gluon sector

- quarks add flavor

quarks add to the picture by 'modifying prefactors' (in accord with dimensional reduction approach)

- no glue \Rightarrow no binding

'glue-free' observables show early onset of perturbative behaviour

Conclusions

- non-perturbative QCD-EoS \sim pure gauge theory EoS
 - the interesting non-perturbative physics in QCD happens in the gluon sector
- nothing qualitatively new in QCD with light quarks
 - quarks add to the picture by 'modifying prefactors' (in accord with dimensional reduction approach) **except close to T_c !!**
- quantum numbers are carried by "quarks" already close to T_c
 - 'glue-free' observables show early onset of perturbative behaviour

Finally...

YES,

- the regime $T_c \leq T \lesssim (1.5 - 2.0)T_c$ differs from the regime $T \gtrsim (1.5 - 2.0)T_c$

It is more difficult (impossible?) to describe it quantitatively in terms of conventional theoretical high-T concepts:
perturbation theory, resummation, dimensional reduction

Finally...

YES,

- the regime $T_c \leq T \lesssim (1.5 - 2.0)T_c$ differs from the regime $T \gtrsim (1.5 - 2.0)T_c$

It is more difficult (impossible?) to describe it quantitatively in terms of conventional theoretical high-T concepts:
perturbation theory, resummation, dimensional reduction

HOWEVER:

- Do we see new physics? \Rightarrow QGL
- or, remnants of old physics? \Rightarrow confinement